DNA transport by a micromachined Brownian ratchet device


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We have micromachined a silicon-chip device that transports DNA with a Brownian ratchet that rectifies the Brownian motion of microscopic particles. Transport properties for a DNA 50-mer agree with theoretical predictions, and the DNA diffusion constant agrees with previous experiments. This type of micromachine could provide a generic pump or separation component for DNA or other charged species as part of a microscale lab-on-a-chip. A device with reduced feature size could produce a size-based separation of DNA molecules, with applications including the detection of single-nucleotide polymorphisms.

The Human Genome Project aims to provide the complete sequence of the 3 billion base pairs of the human genome. While the dominant method for analyzing DNA fragments remains gel electrophoresis, new technologies that have the potential to increase the rate and decrease the cost of DNA sequencing and analysis, such as mass spectrometry and hybridization arrays, are critical to the project's success (1). Here we describe a method of DNA transport and separation based on a Brownian ratchet. As described originally by Smoluchowski (2) and noted by Feynman (3), a Brownian particle can undergo net transport on a potential energy surface that is externally driven to fluctuate between several distinct states. Brownian ratchets have attracted theoretical attention (4–12) because of their description of molecular motors (13–15) and their similarity with phenomena termed stochastic resonance and resonance activation (16, 17).

Brownian ratchets have been demonstrated to transport micrometer- to millimeter-sized particles in experiments with ratchets generated by dielectrophoresis (18), optical tweezers (19), and electrocapillary forces (20, 21). Other devices based on entropic ratchets (22) or physical barriers (23, 24) have been proposed as well. More recently, a geometrical sieve device has been used to separate phospholipids (25).

Despite these successes, the Brownian ratchet mechanism has not before proved capable of transporting DNA fragments in the size ranges applicable to DNA sequencing (<1000 nt) because the interactions used to establish the ratchet potential were too weak. In contrast to previous devices using polarization interactions to generate ratchets (18, 19), the device that we have fabricated uses charge–charge interactions to generate the ratchet potential. As seen below, the charge–charge interactions have sufficient strength to establish ratchets that can trap small DNA fragments.

The ratchet-like wells that trap DNA are generated by charging a series of patterned electrodes. When the electrodes are discharged, the traps vanish and the molecules undergo Brownian motion. Next the potential is reapplied, and the particles again collect in the traps. A spatial asymmetry in the shape of each ratchet-shaped well rectifies the Brownian motion and produces net transport as the on–off cycle is repeated. Each molecule’s transport rate depends on its diffusion constant, allowing the possibility of size-based separations. We have implemented the device by microfabrication on a silicon chip.

This report describes the Brownian ratchet theory, provides a derivation of the transport rate, and presents experimental results for a single sized DNA oligomer. Greater details regarding the fabrication methods and a more extensive presentation of the experimental results for a variety devices and oligomer sizes are available elsewhere (26).

**Theory and Methods**

A silicon wafer with six micromachined devices is shown in Fig. 1, with a schematic design below. The electric potential that creates the ratcheting traps is generated by two arrays of interdigitated electrodes that are perpendicular to the transport axis. The two sets of arrays each extend from bond pads on opposite sides of the device. The spacing between electrodes extending from the same bond pad is \( l \). The asymmetric pattern creates two different spacings, \( r \) and \( l − r \), between electrodes extending from opposite bond pads. The smaller spacing \( r \) defines the feature size of the device.

As also shown in Fig. 1, a simplified one-dimensional description of the potential approximates the electrodes as infinitely thin wires. To simplify the theoretical model, we have neglected the finite width of the electrode, the dependence of the electric potential on the distance normal to the surface, and the corresponding detailed calculation of the potential along the transport axis.

When a voltage difference \( V \) is applied across the two electrode arrays during the on-state, with duration \( t_{\text{on}} \), sawtooth-shaped ratcheting traps are created for charged particles. The electrodes are discharged to \( V = 0 \) during the off-state, with duration \( t_{\text{off}} \), and particles undergo isotropic Brownian diffusion. When the potential is reapplied, the particles are again trapped in potential wells. The times \( t_{\text{on}} \) and \( t_{\text{off}} \) are within the low-frequency, quasistatic approximation; nonadiabatic effects and current reversals, reported elsewhere (27, 28), are not applicable in this regime. Due to the asymmetry of the sawtooth shape and the choice of \( t_{\text{on}} \), a particle starting from well 0 has a measurable probability to be trapped in well 1 and virtually zero probability to be trapped in well 1 and virtually zero probability to be trapped in well −1. Transport can be generated by repetitive cycling between the on-state and the off-state. The transport properties of a particle are determined by its diffusion constant \( D \) and its charge \( Q \), along with the thermal energy \( k_B T \) and the device parameters defined previously.

Each cycle begins by applying the potential \( V \) for a time \( t_{\text{on}} \) that is sufficient to localize particles at the bottoms of the trapping wells. A particle at the barrier-top drifts down the side of the sawtooth of length \( l − r \) to find the bottom of the well, which defines the time required for complete trapping.

**Abbreviation:** SNP, single-nucleotide polymorphism.

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\[ t_{\text{on}} = (l - r)^2 k_B T / Q V D, \]  

\[ \text{[1]} \]

according to overdamped Brownian motion. At the end of the trapping, the particle distribution at the bottom of a well is assumed to be much narrower than the feature size \( r \).

In the next phase of the cycle, the potential is turned off for time \( t_{\text{off}} \). When the potential is reapplied, particles that have diffused farther than the barrier to the left (roughly distance \( l \) away) will hop to the previous well, and particles that have diffused farther than the barrier to the right (roughly distance \( r \) away) will be transported to the next well. Since \( r < l \), we can choose an intermediate time \( t_{\text{off}} \) such that \( t_{\text{off}} \sim r^2 / 2D \ll l^2 / 2D \) and particles always move right, never left.

To compute the probability \( \alpha \) that a particle moves one well to the right in a single cycle, we note that the effective distance \( r_{\text{eff}} \) it must travel is between \( r \) (the inner edge-to-edge distance between electrodes) and \( 3r \) (the outer edge-to-edge distance).

The probability distribution (or equivalently Green's function) for a particle starting at the origin undergoing one-dimensional Brownian motion for time \( t_{\text{off}} \) is

\[ P(x; t_{\text{off}}) = \frac{\exp[-x^2 / 4D t_{\text{off}}]}{\sqrt{4\pi D t_{\text{off}}}}. \]  

\[ \text{[2]} \]

An expression for \( \alpha \) is then obtained by integrating \( P(x; t_{\text{off}}) \) from \( r_{\text{eff}} \) to infinity:

\[ \alpha = \frac{1}{2} \text{erfc}(\sqrt{r_{\text{eff}}^2 / 4D t_{\text{off}}}) = \frac{1}{2} \text{erfc}(\sqrt{r^2 / 2D t_{\text{off}}}). \]  

\[ \text{[3]} \]

The distance \( r_{\text{eff}}^2 \) has been written in terms of the characteristic diffusion time \( 2D t_c \), where \( t_c = r_{\text{eff}}^2 / 2D \) is the time required to diffuse a distance equal to the short side \( r_{\text{eff}} \) of the trapping well. In this derivation, we assumed that \( t_{\text{off}} \) is short enough that
particles diffuse less than a single ratchet—i.e., \( P(x; t_{\text{off}}) \approx 0 \) for \( x > l \). An expression for \( \alpha \) valid in the limit of large \( t_{\text{off}} \) is \( \alpha = \sum_{k=-\infty}^{\infty} \int_{x_{\text{eff}}}^{x_{\text{eff}}+\sigma^2(n)} P(x; t_{\text{off}}) \),

\[
\begin{align*}
\sigma^2(n) &= n^2(1 - \alpha). \quad [4b] \\
\alpha &= \frac{\alpha_{eff}}{t_{\text{on}} + t_{\text{off}}} \quad [5]
\end{align*}
\]

are plotted in Fig. 2. The transport fraction \( \alpha \) (black line) increases with \( t_{\text{off}} \) and approaches a maximum value of 1/2 when back-diffusion is neglected. The flux in units of the characteristic time \( t_s \) is \( \alpha/(t_{\text{on}} + t_{\text{off}}) \) and is shown for \( t_{\text{on}} = t_{\text{off}}/3 \) (gray line). The flux is reminiscent of a stochastic resonance with a maximum when \( t_{\text{off}} = t_s \).

According to Eq. 1, the expected time required to focus a DNA 50-mer is 0.006 sec, based on a thermal energy of 26 meV, a charge of 1e− per nucleotide yielding \( QV = 80 \) eV, and a diffusion constant of \( 1.8 \times 10^{-7} \) cm²/sec [estimated from a rhodamine-labeled 30-mer on a quartz surface (3)]. We visually ascertained that the switching time \( t_{\text{on}} \) was sufficient to permit complete focusing of the DNA on the positive electrodes, even for the fastest switching rate of 8 Hz (\( t_{\text{on}} = 0.03 \) sec).

Results and Discussion

In Fig. 3 we show three images from a typical experiment using a device with 2-μm electrodes and a 0.7-Hz switching frequency to transport a rhodamine-labeled DNA 50-mer. These images were saved during the trapping phase of the cycle, and fluorescence maxima are clearly seen from DNA molecules captured on the positive electrodes. At the start of the experiment, the DNA oligomers are focused on left-most three electrodes. As the potential cycles between on- and off-states, the packet moves to the right and broadens.
the right and broadens. The transport rate $\alpha$ can be estimated by noting that the intensity maximum moves from electrode 1 to electrode 3 after 10 cycles, then to electrode 5 after 10 more cycles, yielding $\alpha \approx 0.2$. For a more precise value, we extracted the intensity profile across the image, set a baseline at the 85th percentile of intensity, calculated the average position $x(n)$ from the intensity above baseline, normalized $x(n)$ by the 10-pixel spacing between electrodes, then measured the slope of $x(n)$ to obtain $\alpha$. For this experiment $\alpha = 0.18$.

The square width also increases linearly with the number of cycles (data not shown); because we used a baseline threshold that narrows the width of the distribution, however, the formula of Eq. 4b no longer provides an accurate relationship between $\sigma^2(n)$ and $\alpha$.

Fig. 4 shows the experimental results for $\alpha$, along with $\pm 1\sigma$ error bars from repeated runs. As predicted, $\alpha$ decreases with increasing frequency. Also shown in Fig. 4 is a theoretical curve from Eq. 3. Least-squares fitting to the data from all but the highest frequency yielded $D(r/r_{eff})^2 = 3.5 \times 10^{-8} \text{cm}^2/\text{sec}$. The good agreement between the experimental results and the single-parameter theoretical fit supports our conclusion that transport is due to a Brownian ratchet.

Furthermore, since $r_{eff} = (2-3)r$, we find that $D = 1.4-3 \times 10^{-7} \text{cm}^2/\text{sec}$. This indirect measure of the diffusion constant brackets the estimated diffusion constant for a DNA 50-mer close to a glass surface, $1.8 \times 10^{-7} \text{cm}^2/\text{sec}$ (30).

The experimental results demonstrating transport permit an examination of the feasibility of fabricating a device to provide useful size-based separations of DNA. Separating two chemical species requires that they have different diffusion constants $D$ and $D'$ and different hopping probabilities $\alpha$ and $\alpha'$. The resolution between the species, defined as

$$\text{resolution} = \frac{|x(n) - x'(n)|}{0.5 \cdot [\alpha(n) + \alpha'(n)]}$$

improves as $n^{1/2}$. The number of cycles required to reach the resolution of 1 typical for DNA separation applications is

$$n = \frac{\alpha(1 - \alpha)}{(\alpha - \alpha')^2},$$

where we have assumed that the two packets acquire a similar width. The separation parameter $t_{off}$ (and, through $t_{off}$, the quantities $\alpha$ and $\alpha'$) can be selected to optimize various quantities associated with a resolved separation—for example, the device length, approximately $l \times [\alpha/(\alpha - \alpha')]^2$, or the total separation time, $n \times (t_{on} + t_{off})$.

A typical application requiring the separation of DNA fragments is the analysis of single nucleotide polymorphisms (SNPs). An SNP is a position in the genome where multiple nucleotides are likely. Characterizing genetic diversity through SNPs has applications including the identification of genes for disease inheritance and susceptibility, the development of personalized medicines, and the documentation of human evolutionary history and migrations through a genetic record (31–34). Preliminary sets of thousands of SNPs, identified by the 12 nt on either side of a polymorphism, have been reported (35). Validating and detecting these SNPs can be accomplished by resequencing specific 25-nt regions of the genome.

Here we investigate the use of a Brownian ratchet device for the resequencing and detection application. Calculations are based on a device with feature size $r = 0.1 \mu m$, periodicity 1 $\mu m$, and a potential difference of 0.1 V between electrodes in the on-state. We estimate the effective DNA diffusion constant $D(r/r_{eff})^2$ from the theoretical scaling for a self-avoiding walk, $D = (\text{length})^{-0.6}$ (36, 37), and our experimental results for the 50-mer. The persistence length of single-stranded DNA is 4 nm, or $13.6 \mu m$ (38), indicating that the self-avoiding walk should be adequate (although not quantitative) for fragment sizes we consider.

The detection of an SNP requires, at most, the ability to sequence the 25-nt region surrounding the polymorphism, which can be accomplished by separating a DNA 24-mer from a 25-mer. Using the theoretical scaling of diffusion constant with DNA length, we extrapolate $D(r/r_{eff})^2$ of $5.44 \times 10^{-8} \text{cm}^2/\text{sec}$ and $5.31 \times 10^{-8} \text{cm}^2/\text{sec}$ for the 24-mer and 25-mer. The time required to focus the DNA at the start of each cycle is $t_{on} = 1.8 \times 10^{-4}$ sec. The optimized separation parameters, calculated by using Eq. 7, require $t_{off} = 2.5 \times 10^{-4}$ sec and 12,000 cycles for a total separation time of 5.4 sec on a 1.25-cm chip.

In conclusion, we have fabricated a Brownian ratchet device that is capable of transporting small DNA molecules in aqueous solution, rather than the inconvenient gel and polymer solutions required for electrophoresis. This type of device could be used as a pump component for transport or separation of charged species in a microfabricated analysis chip. Multiple miniaturized devices can also be arrayed side-by-side for high-throughput operation. On the basis of experimental measurements, we suggest the feasibility of using this type of device for biological applications, for example the validation of SNPs.

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